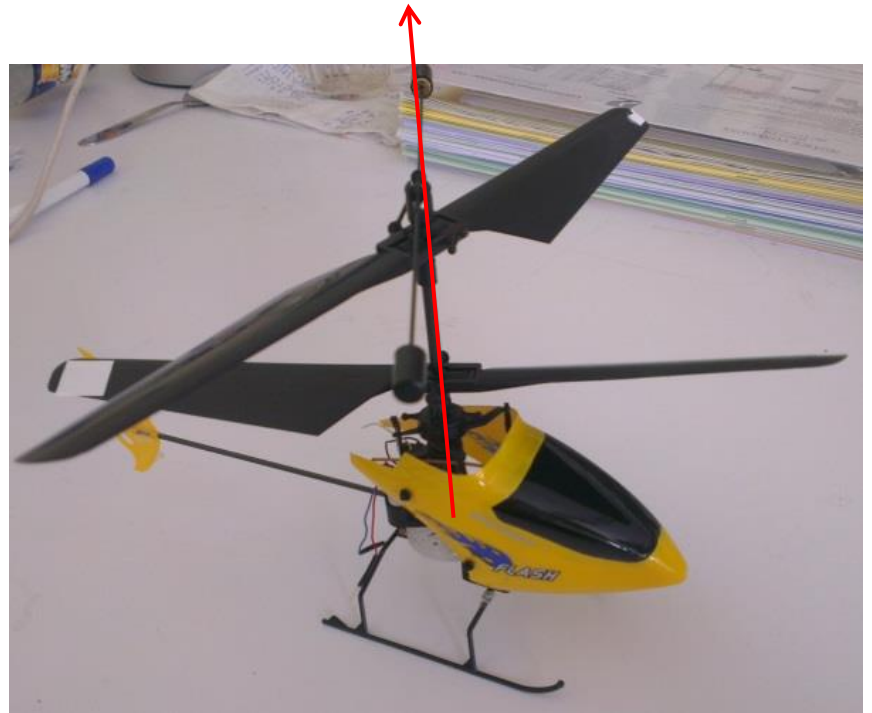


Hélicoptère birotor

1) Du système réel à la maquette

2) Modélisation

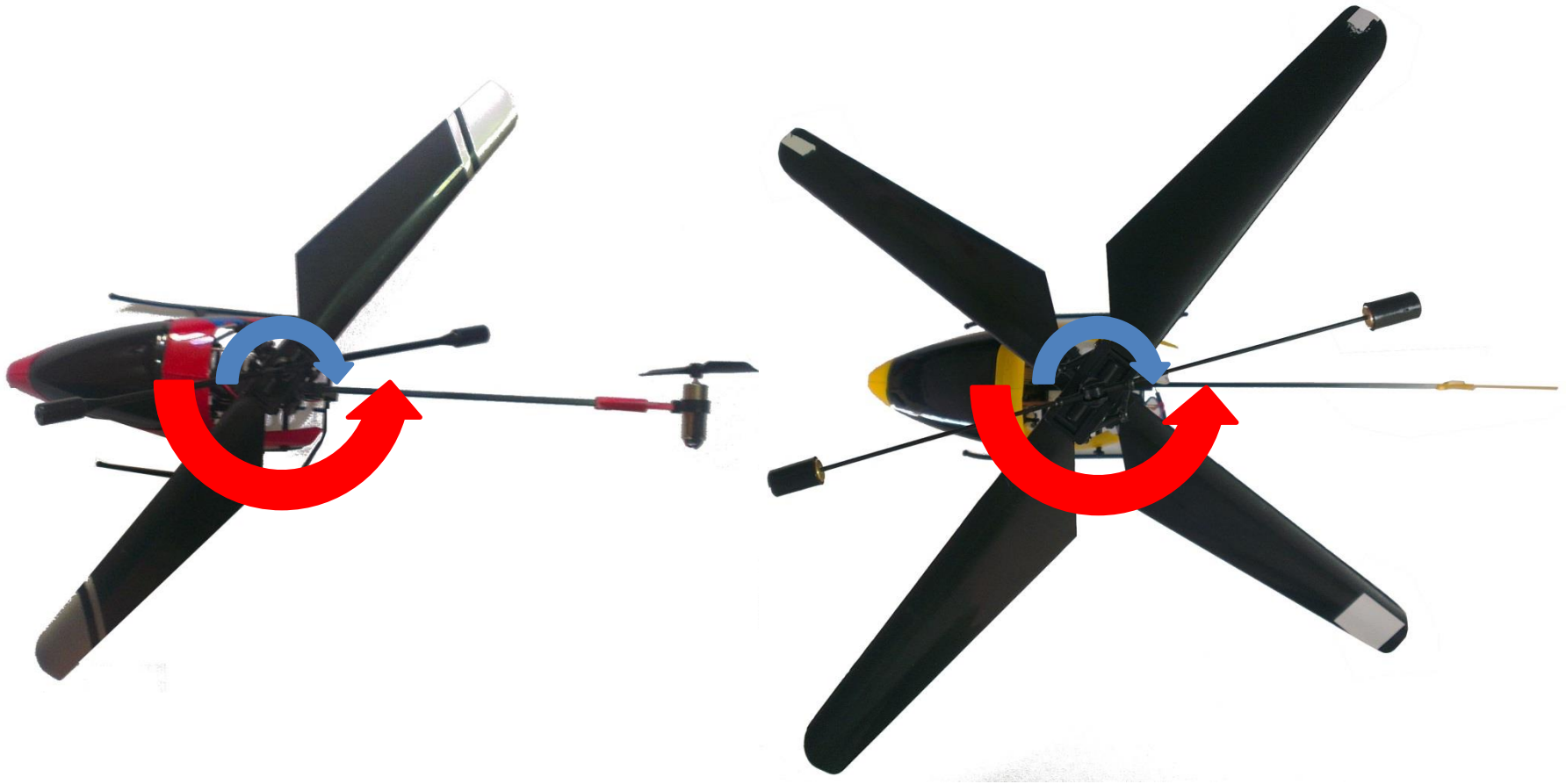
3) Asservissement



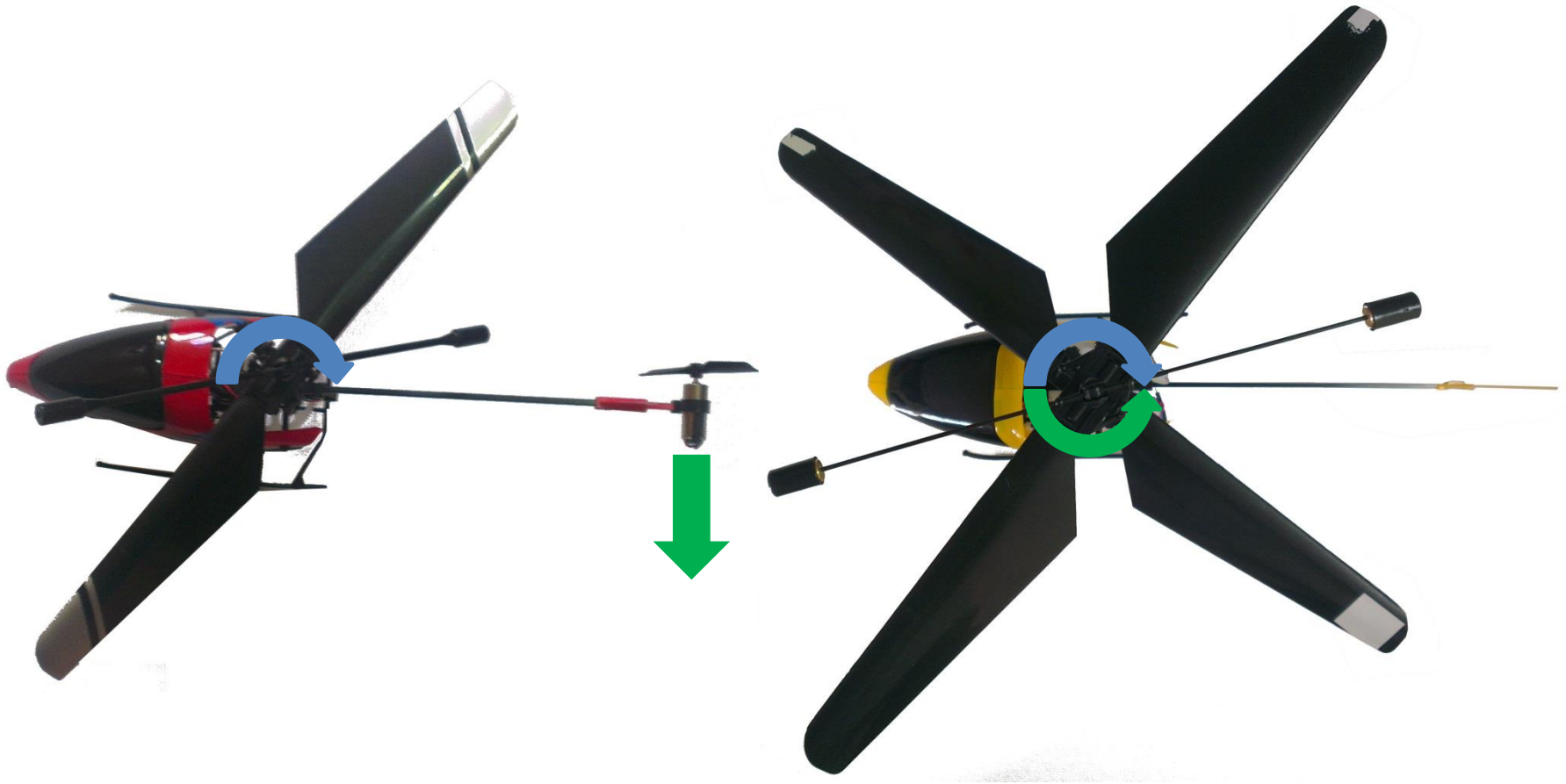
a) Système réel



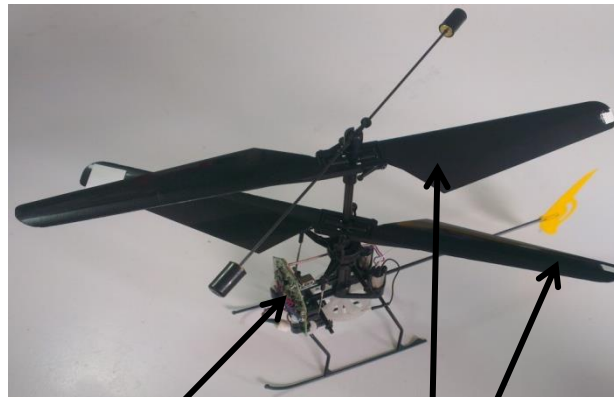
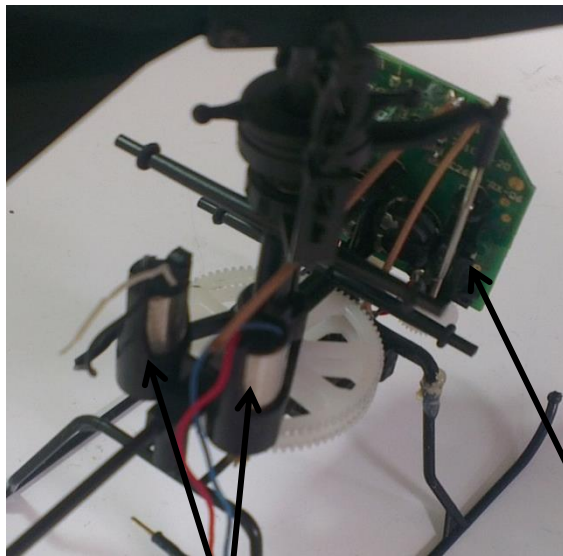
a) Système réel



a) Système réel



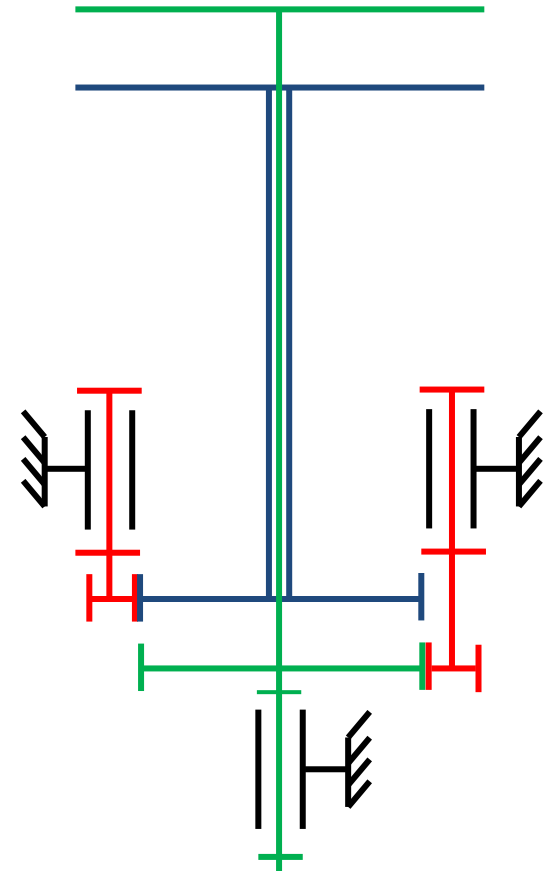
a) Système réel



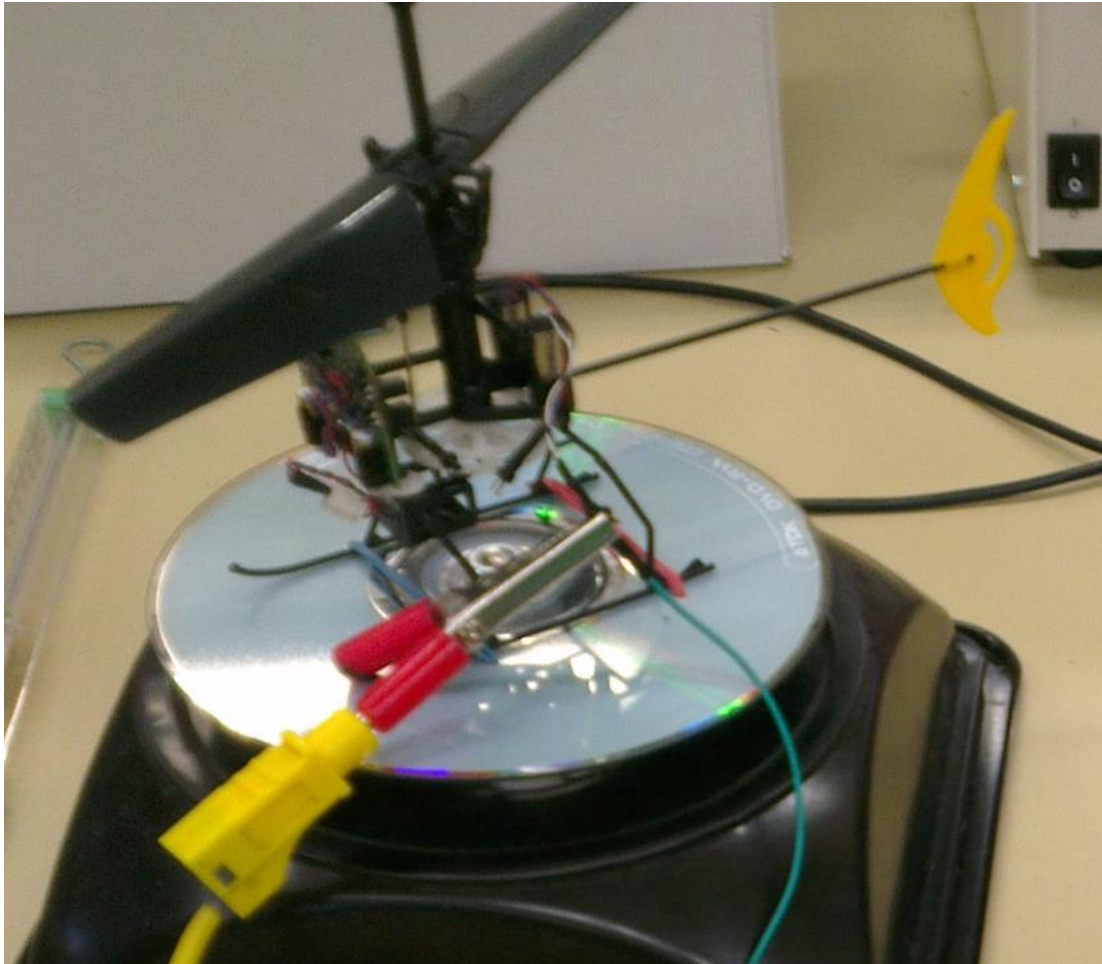
Moteurs

Carte de commande

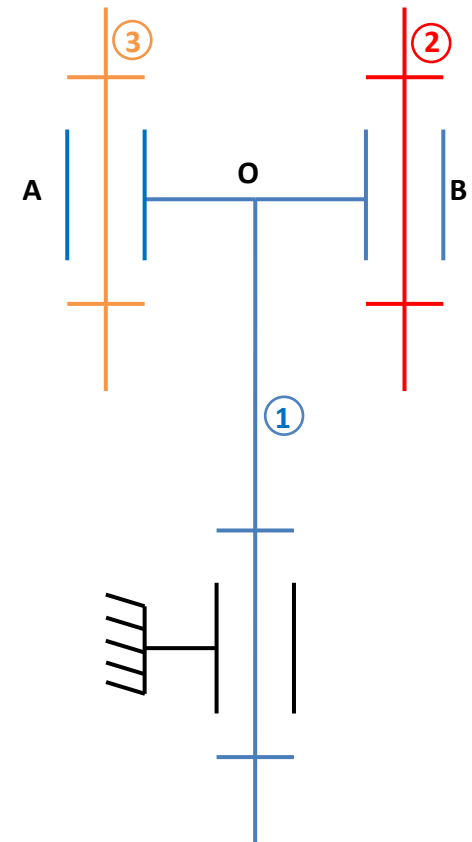
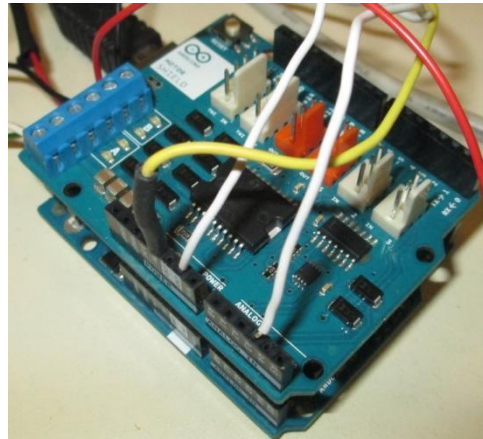
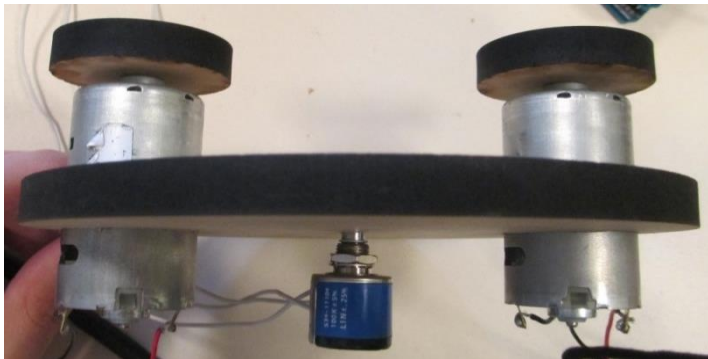
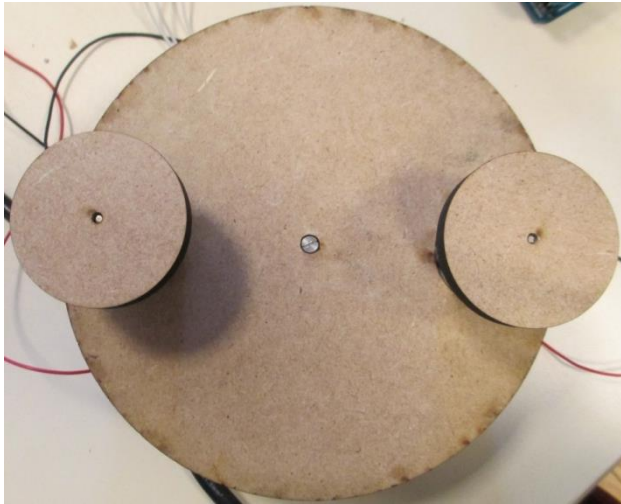
Rotors



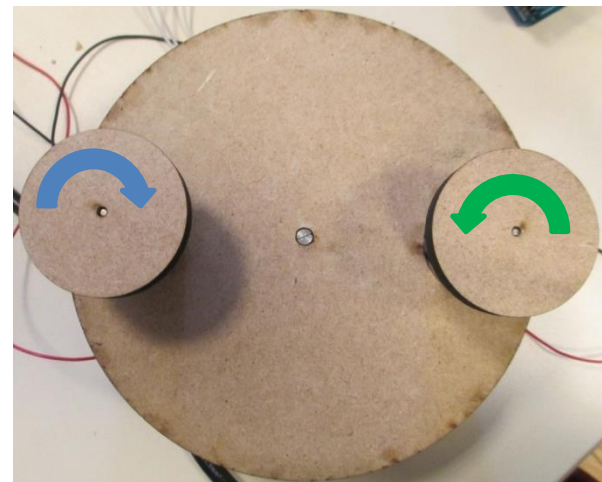
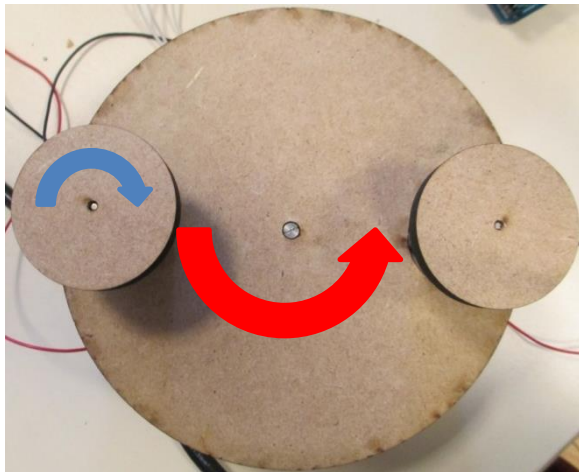
a) Système réel



a) Système réel



b) Maquette



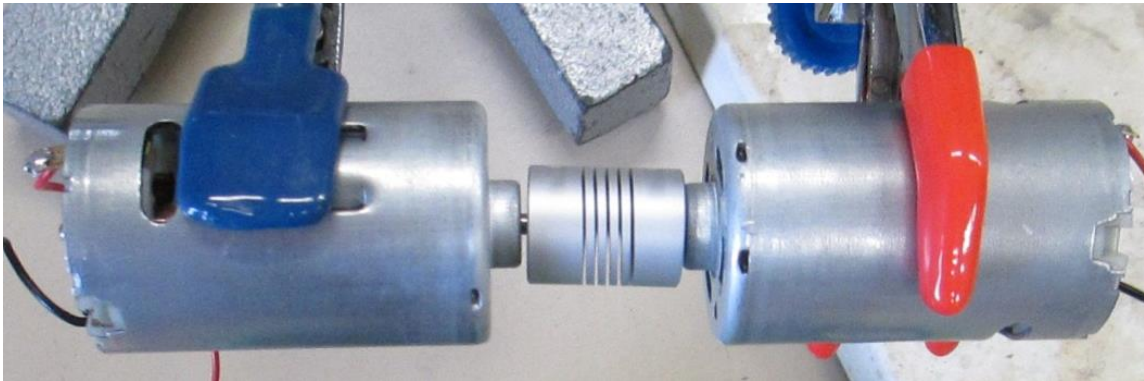
a) Caractéristiques des moteurs

- Dans un moteur à courant continu :

$$U(t) = K_e \cdot \omega(t) + R i(t) + L \frac{di}{dt}$$

$$J_{\text{mot}} \frac{d\omega}{dt} = K_c \cdot i(t) - C_r(t)$$

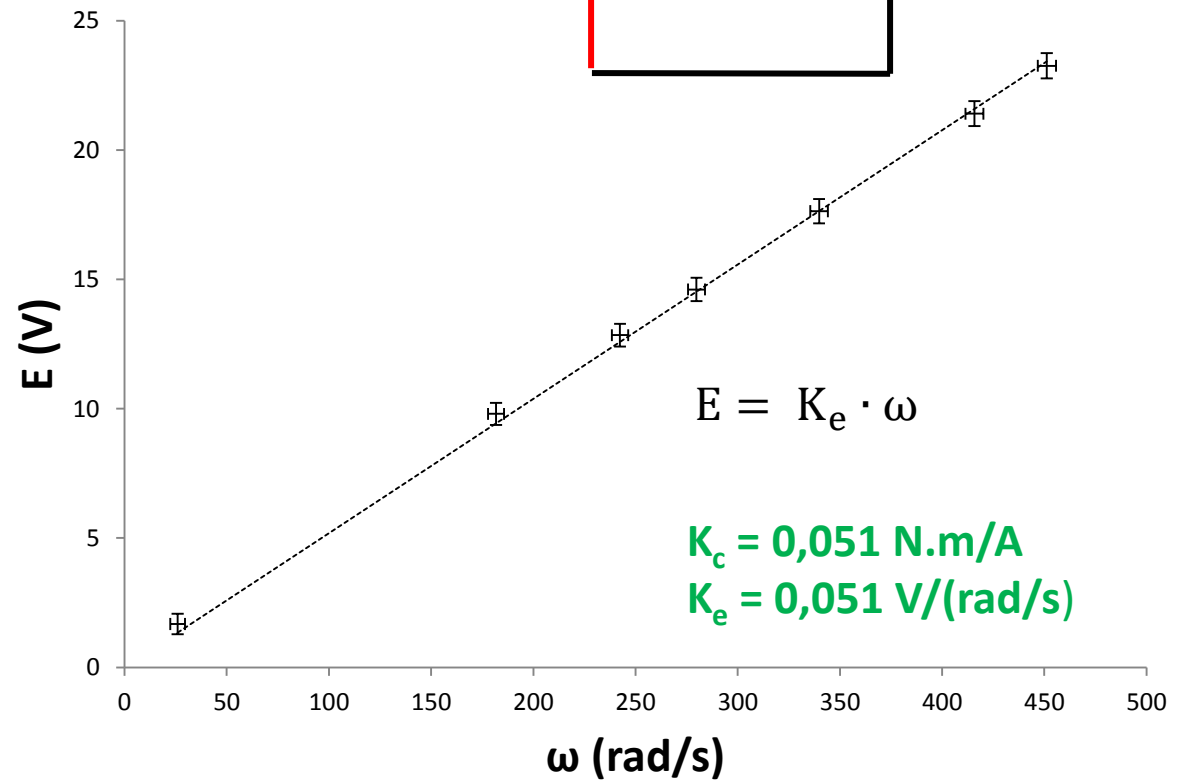
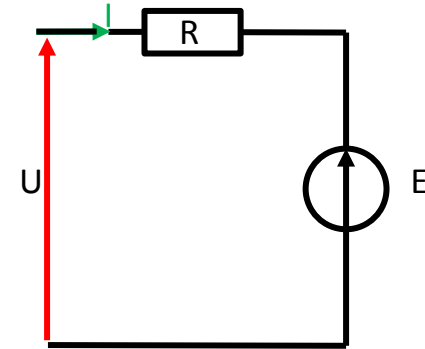
- On néglige l'inductance : $L = 0 \text{ H}$
- En bloquant le rotor : $R = 9,96 \pm 0,12 \Omega$



a) Caractéristiques des moteurs



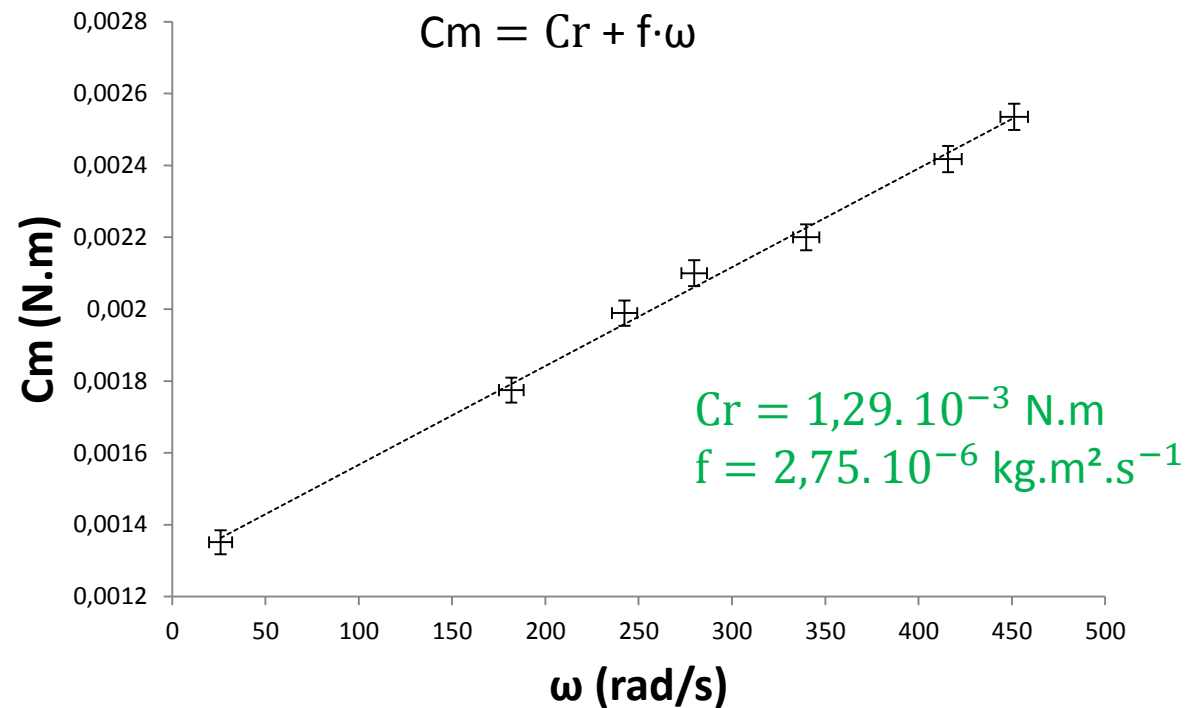
Essai à vide :



a) Caractéristiques des moteurs



Essai à vide :



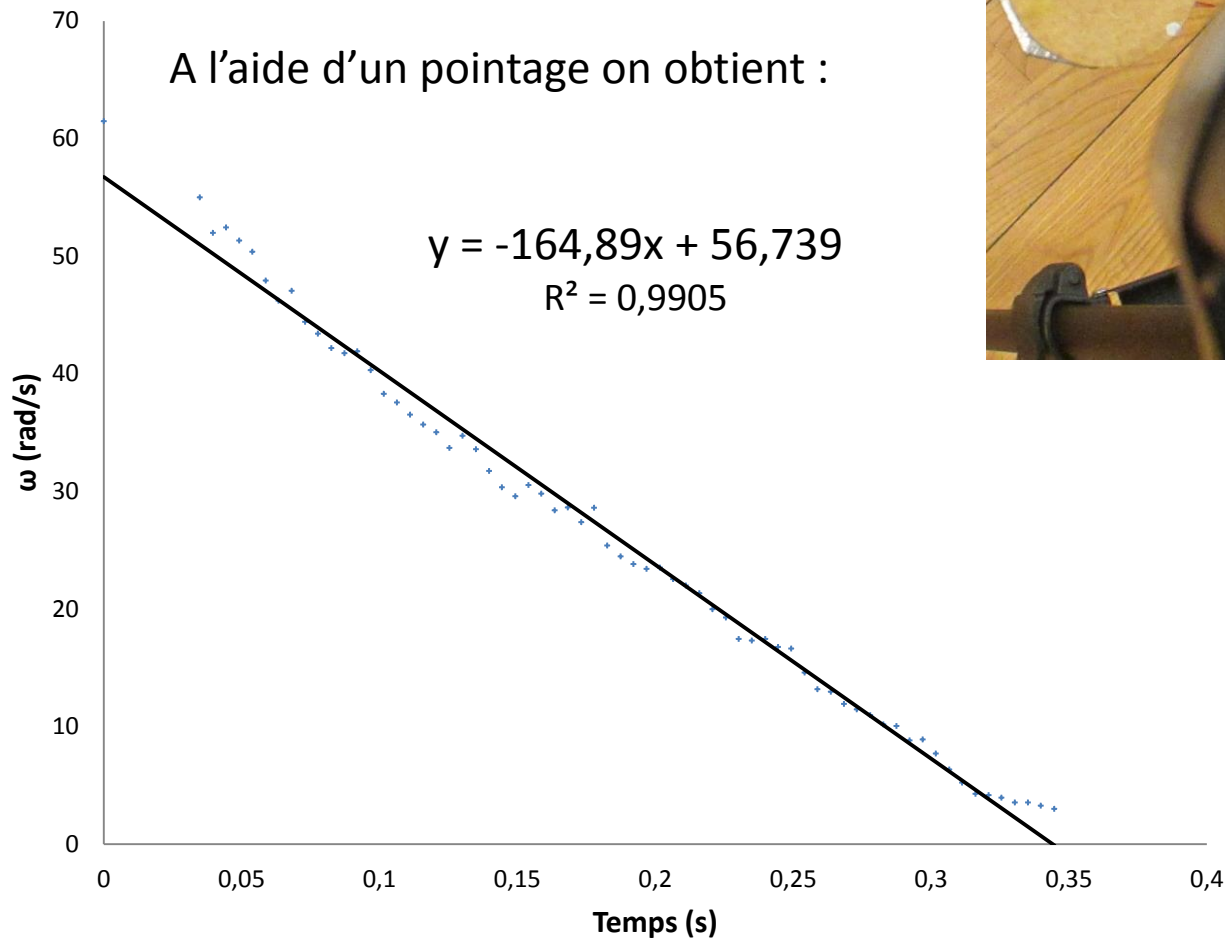
a) Caractéristiques des moteurs

- On effectue un essai de lâcher:

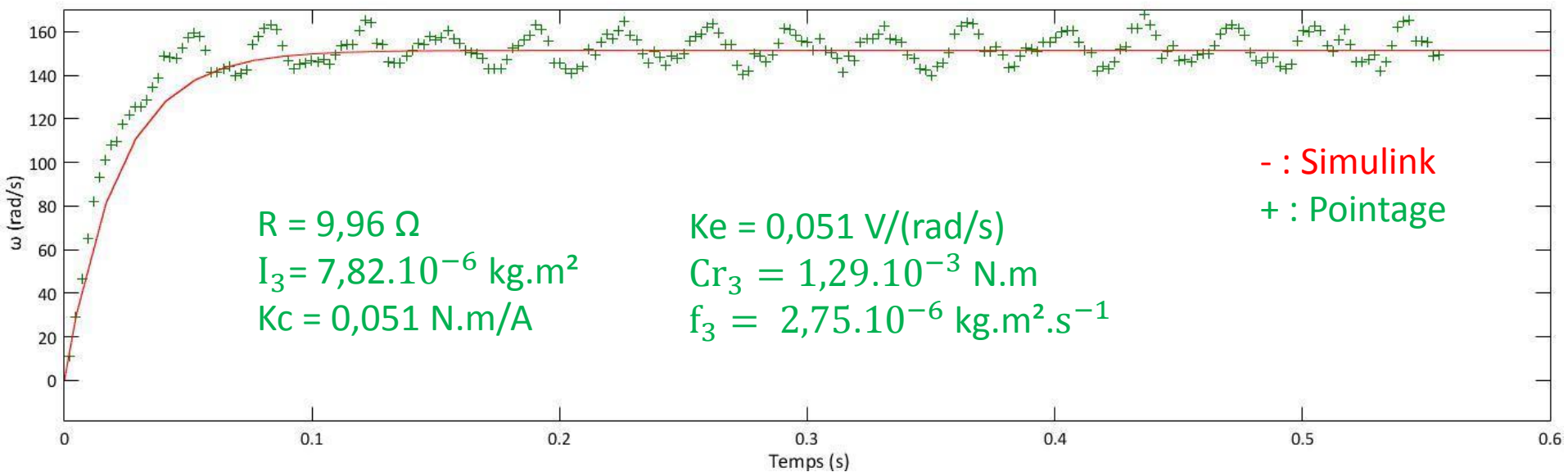
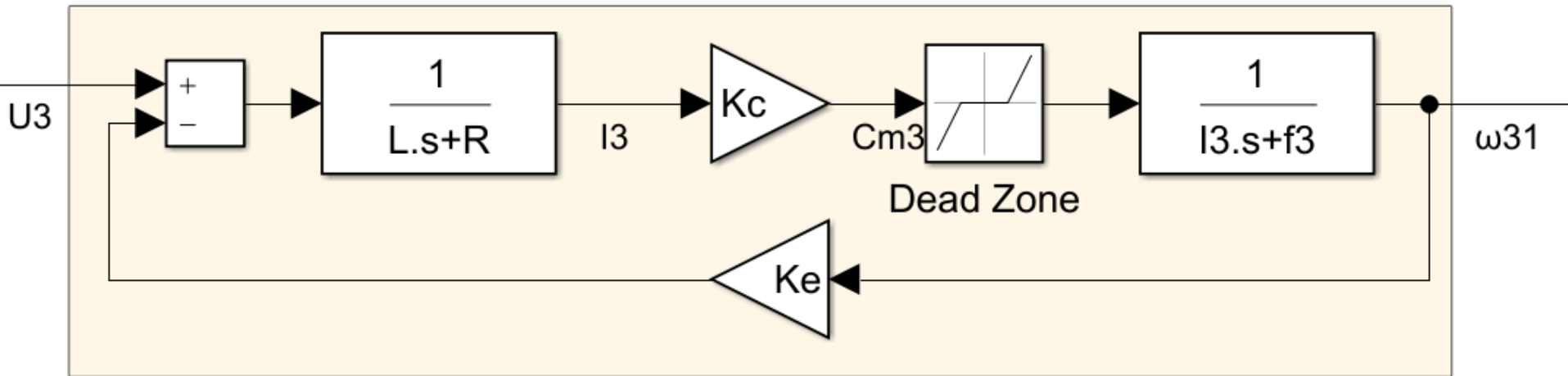
$$I_2 \frac{d\omega}{dt} = -Cr_2(t)$$

A l'aide d'un pointage on obtient :

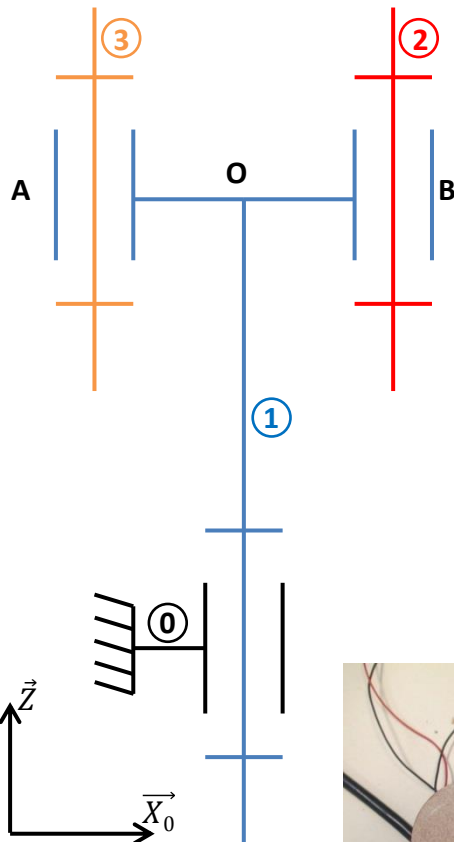
$$y = -164,89x + 56,739$$
$$R^2 = 0,9905$$



Donc : $I_2 = I_3 = 7,82 \cdot 10^{-6} \text{ kg.m}^2$



b) Caractéristiques du plateau



On isole {3} (respectivement {2})

Théorème du moment dynamique en A suivant \vec{z} :

$$I_3 \dot{\omega}_{31}(t) = C m_3(t) - C r_3(t) - f_3 \omega_{31}(t) - I_3 \dot{\omega}_{10}(t)$$

$$I_2 \dot{\omega}_{21}(t) = C m_2(t) - C r_2(t) - f_2 \omega_{21}(t) - I_2 \dot{\omega}_{10}(t)$$

On isole {1+2+3}

Théorème du moment dynamique en O suivant \vec{z} , en posant

$$I_{eq} = I_1 + I_2 + m_2 \cdot r_2^2 + I_3 + m_3 \cdot r_3^2 :$$

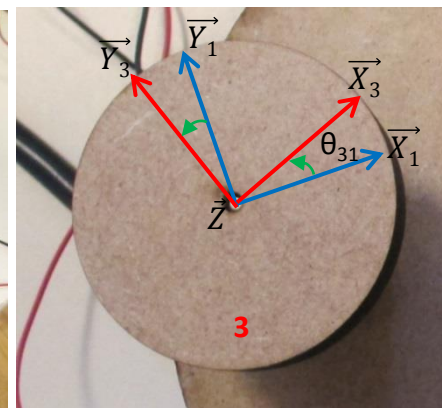
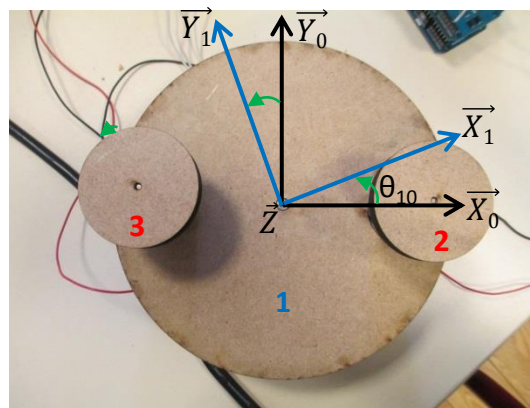
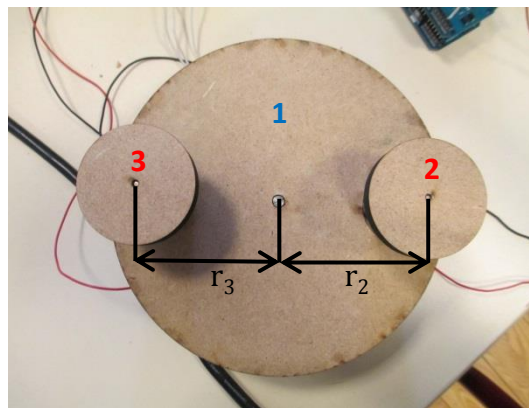
$$I_{eq} \dot{\omega}_{10}(t) = -I_2 \dot{\omega}_{21}(t) - I_3 \dot{\omega}_{31}(t) - C r_1(t) - f_1 \omega_{10}(t)$$

Longueurs :

$$\overrightarrow{OB} = r_2 \cdot \vec{x}_1;$$

$$\overrightarrow{OA} = -r_3 \cdot \vec{x}_1$$

$$r_3 = r_2$$



b) Caractéristiques du plateau

On considère les composants comme des cylindres d'épaisseur $e = 8 \text{ mm}$.

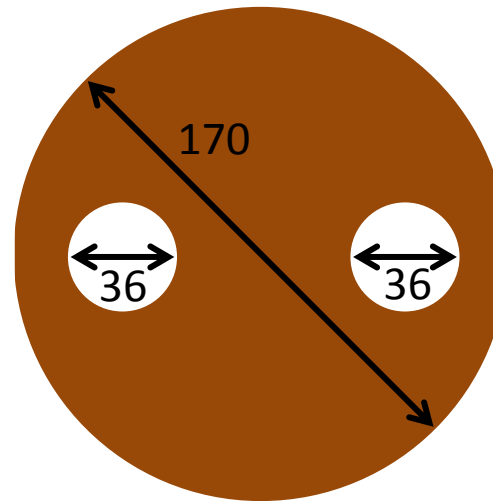
Masses :

$$M_{\text{moteur}} = 210,7 \text{ g}$$

$$M_{\text{volant}} = 12,8 \text{ g}$$

$$M_{\text{plateau}} = 130,8 \text{ g}$$

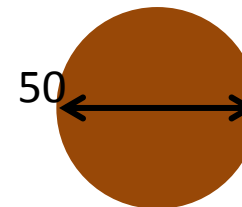
Plateau



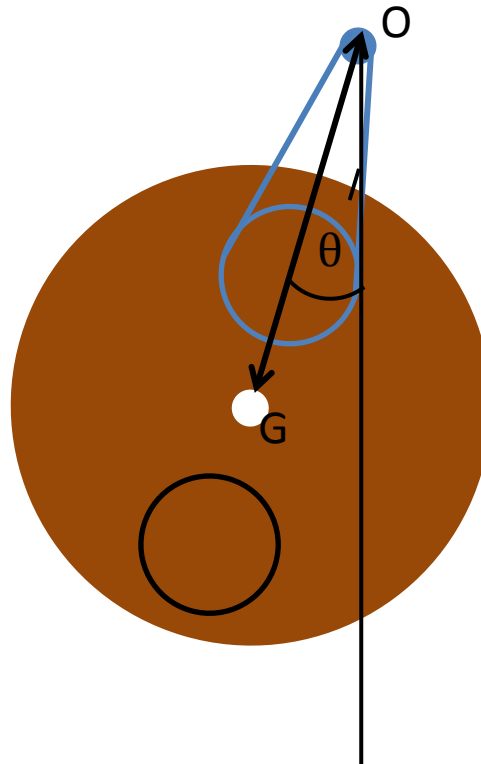
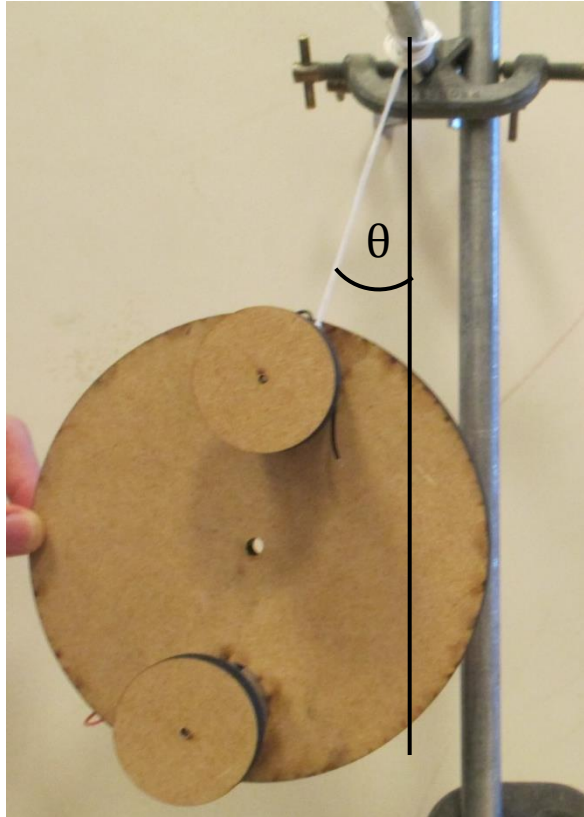
$$\text{Plateau : } I_1 = 2,05 \cdot 10^{-3} \text{ kg.m}^2$$

$$\text{Inertie équivalente : } I_{\text{eq}} = 3,6 \cdot 10^{-3} \text{ kg.m}^2$$

Volants d'inertie



b) Caractéristiques du plateau



On mesure la période d'oscillation de l'ensemble, et on en déduit le moment d'inertie en O, on le transporte en G :

$$J = mgl * \frac{T^2}{4\pi^2}$$

On mesure :

$$T = 0,70 \text{ s}$$

$$l = 0,098 \text{ m}$$

$$m = 0,552 \text{ kg}$$

$$\text{Donc } I_{eq} = 1,4 \cdot 10^{-3} \text{ kg.m}^2$$

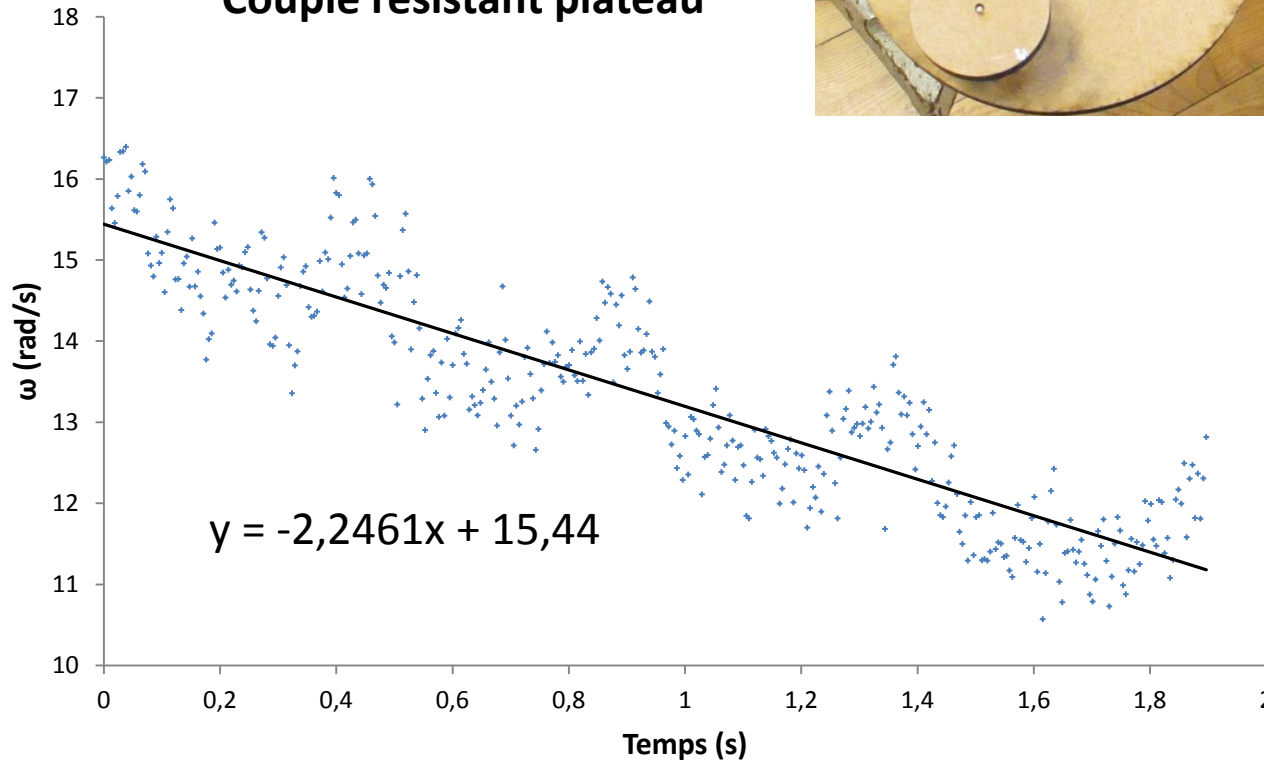
$$I_{eq} = I_1 + I_2 + I_3 + m_2 \cdot r_2^2 + m_3 \cdot r_3^2$$

b) Caractéristiques du plateau

- $I_{eq} \frac{d\omega}{dt} = Cr_1(t)$

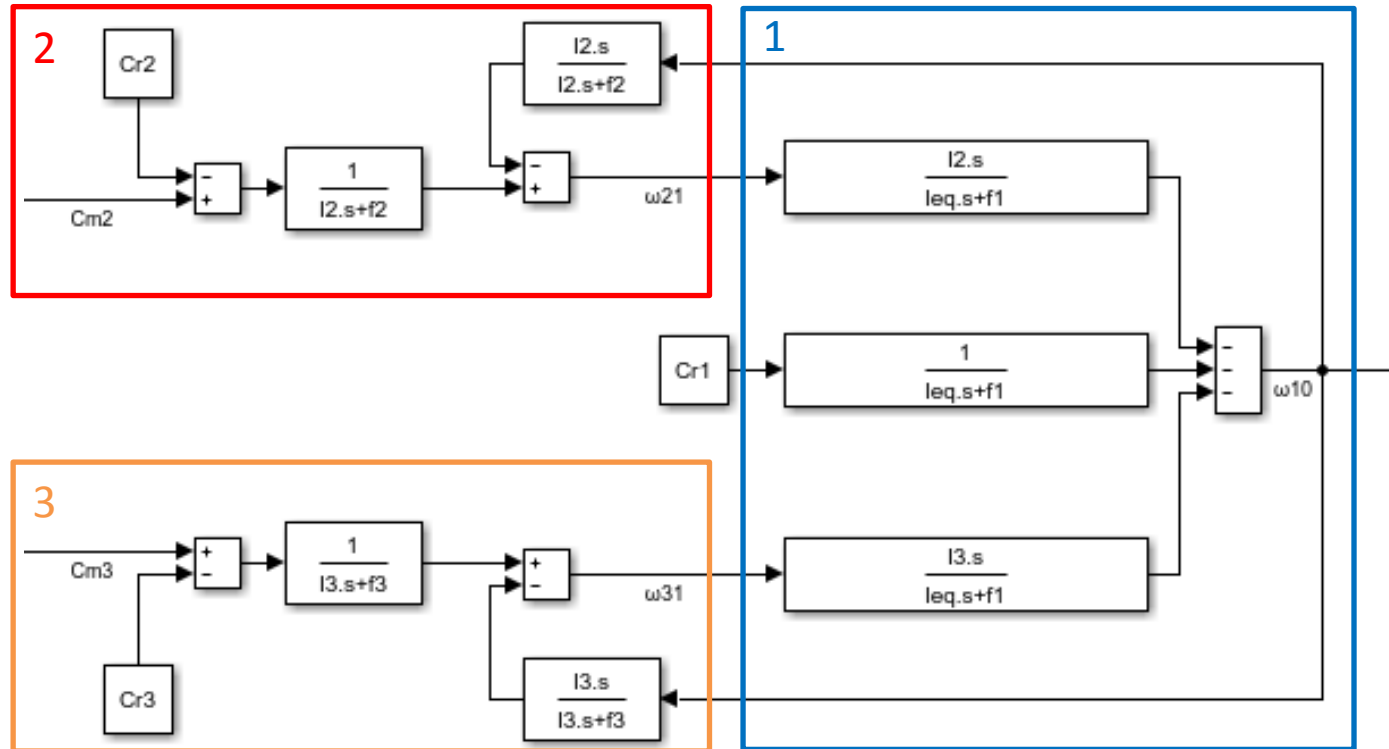


Couple résistant plateau



Donc : $Cr_1 = 8.10^{-3} \text{N.m}$

b) Caractéristiques du plateau



$$I_2 = I_3 = 7,82 \cdot 10^{-6} \text{ kg.m}^2$$

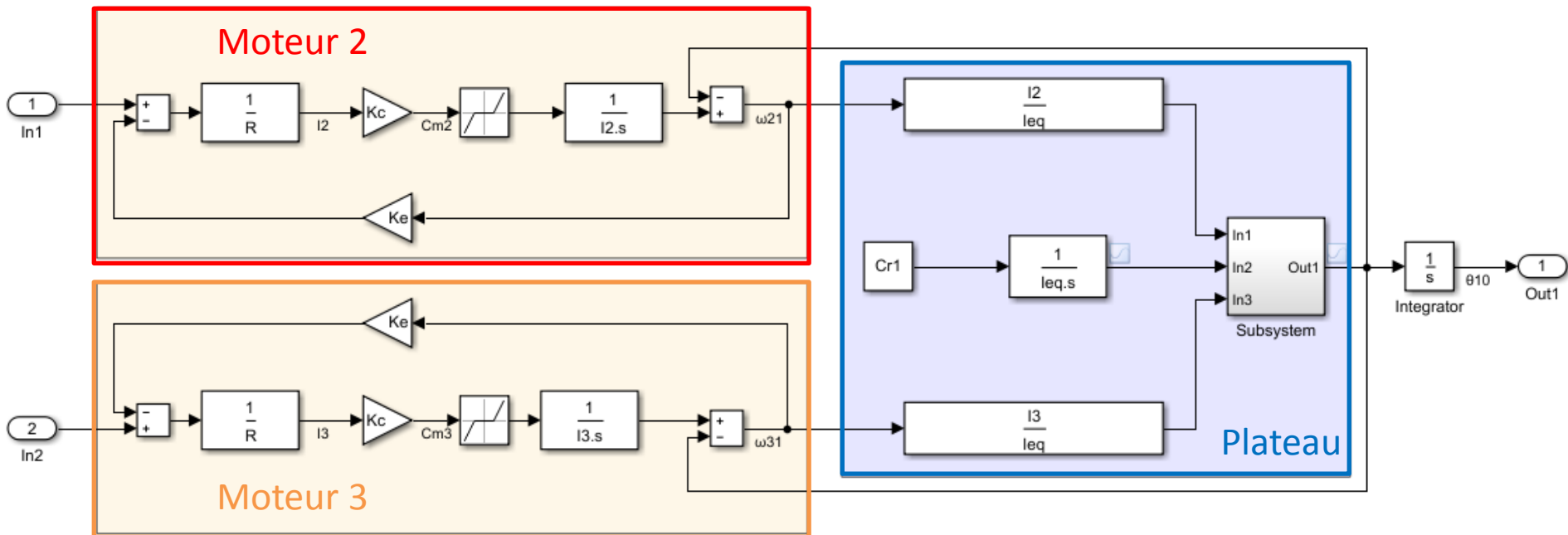
$$I_{eq} = 3,6 \cdot 10^{-3} \text{ kg.m}^2$$

$$Cr_2 = Cr_3 = 1,29 \cdot 10^{-3} \text{ N.m}$$

$$Cr_1 = 8 \cdot 10^{-3} \text{ N.m}$$

$$f_2 = f_3 = 2,75 \cdot 10^{-6} \text{ kg.m}^2 \cdot \text{s}^{-1}$$

c) Validation



$$R = 9,96 \, \Omega$$

$$K_c = 0,051 \, \text{N.m/A}$$

$$K_e = 0,051 \, \text{V/(rad/s)}$$

$$I_1 = 2,05 \cdot 10^{-3} \, \text{kg.m}^2$$

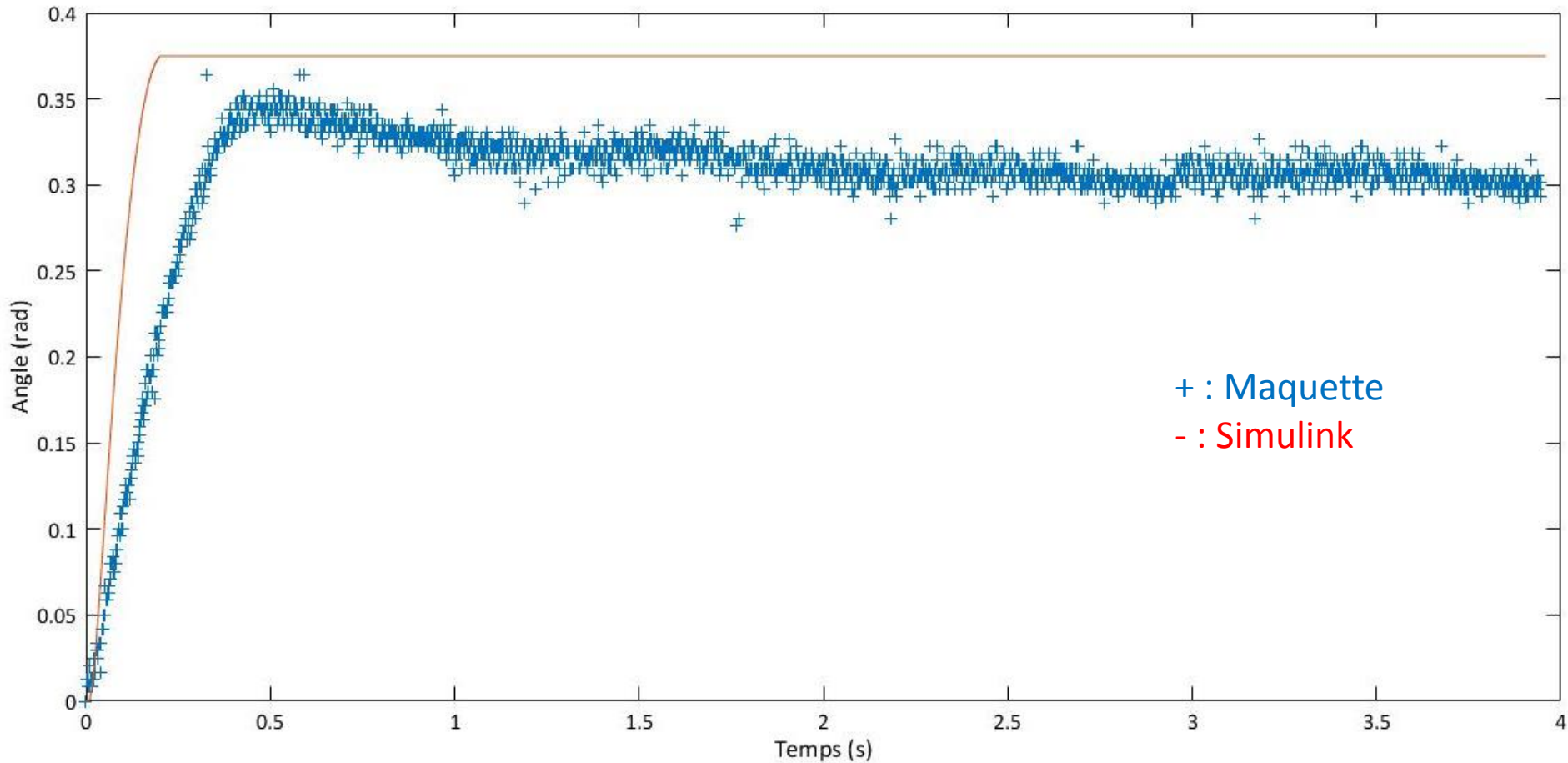
$$I_2 = I_3 = 4,18 \cdot 10^{-6} \, \text{kg.m}^2$$

$$I_{eq} = 3,6 \cdot 10^{-3} \, \text{kg.m}^2$$

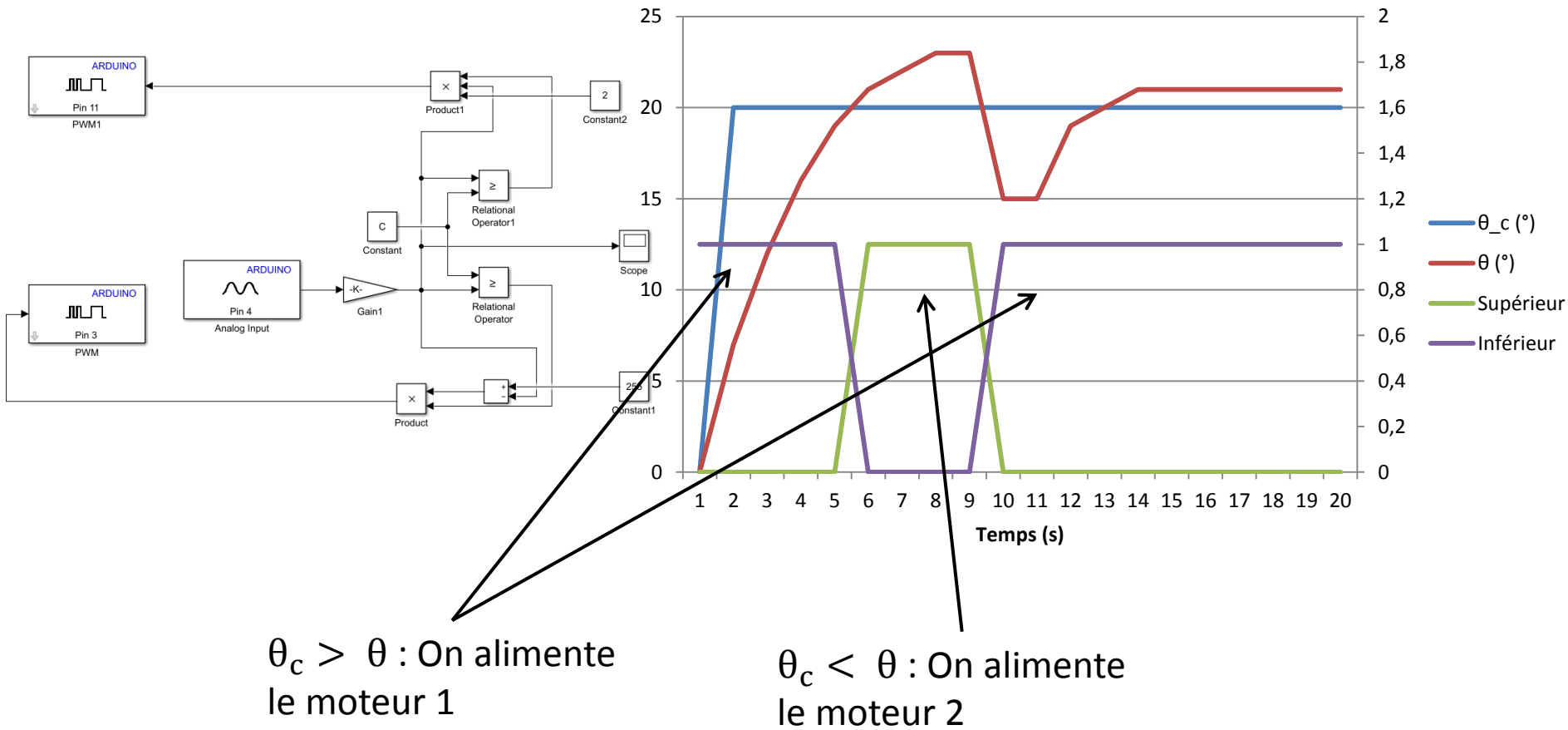
$$Cr_1 = 0,008 \, \text{N.m}$$

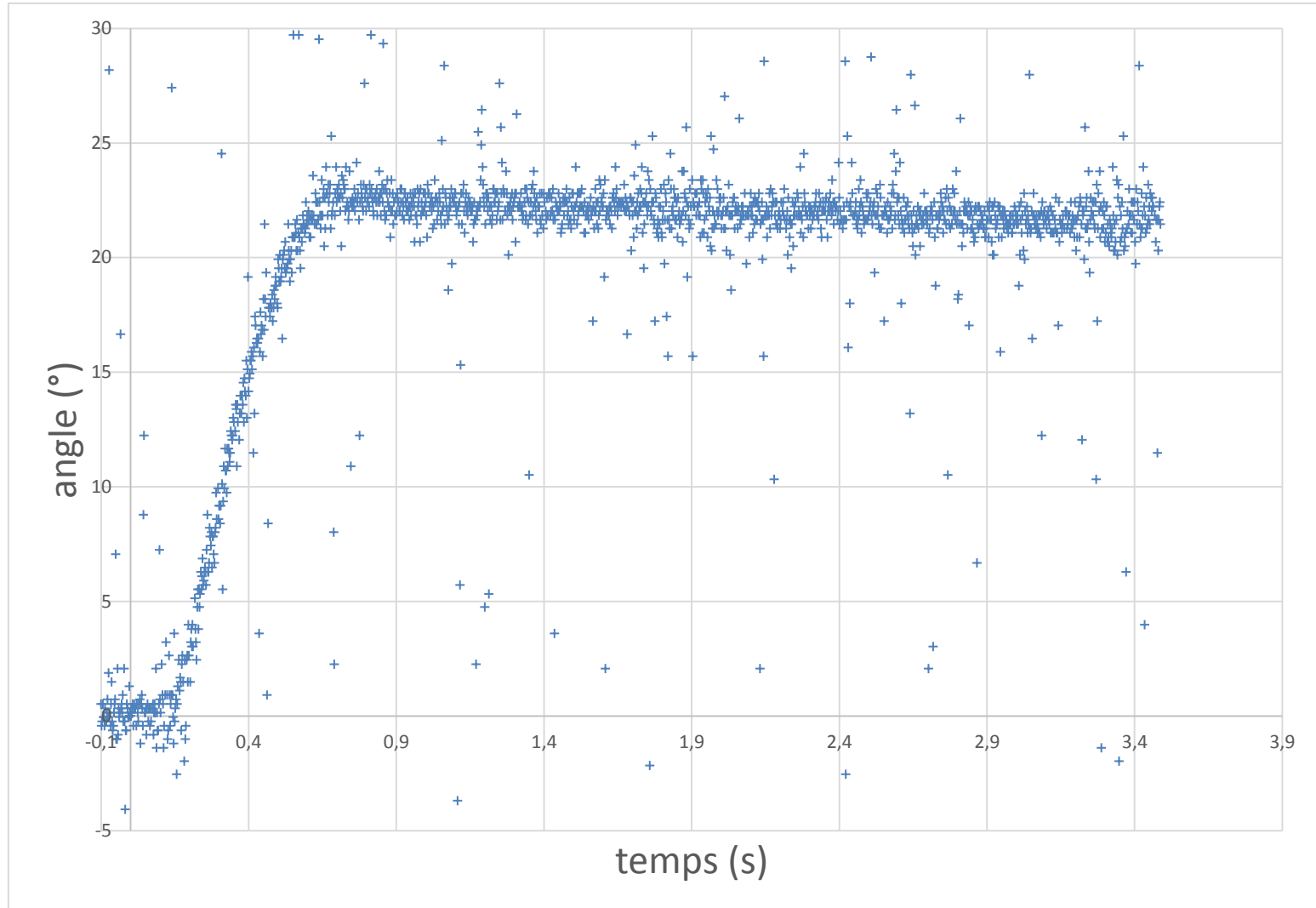
$$Cr_2 = Cr_3 = 0,0007 \, \text{N.m}$$

c) Validation



a) Avec MatLab



a) Avec MatLab

b) Avec Arduino

```

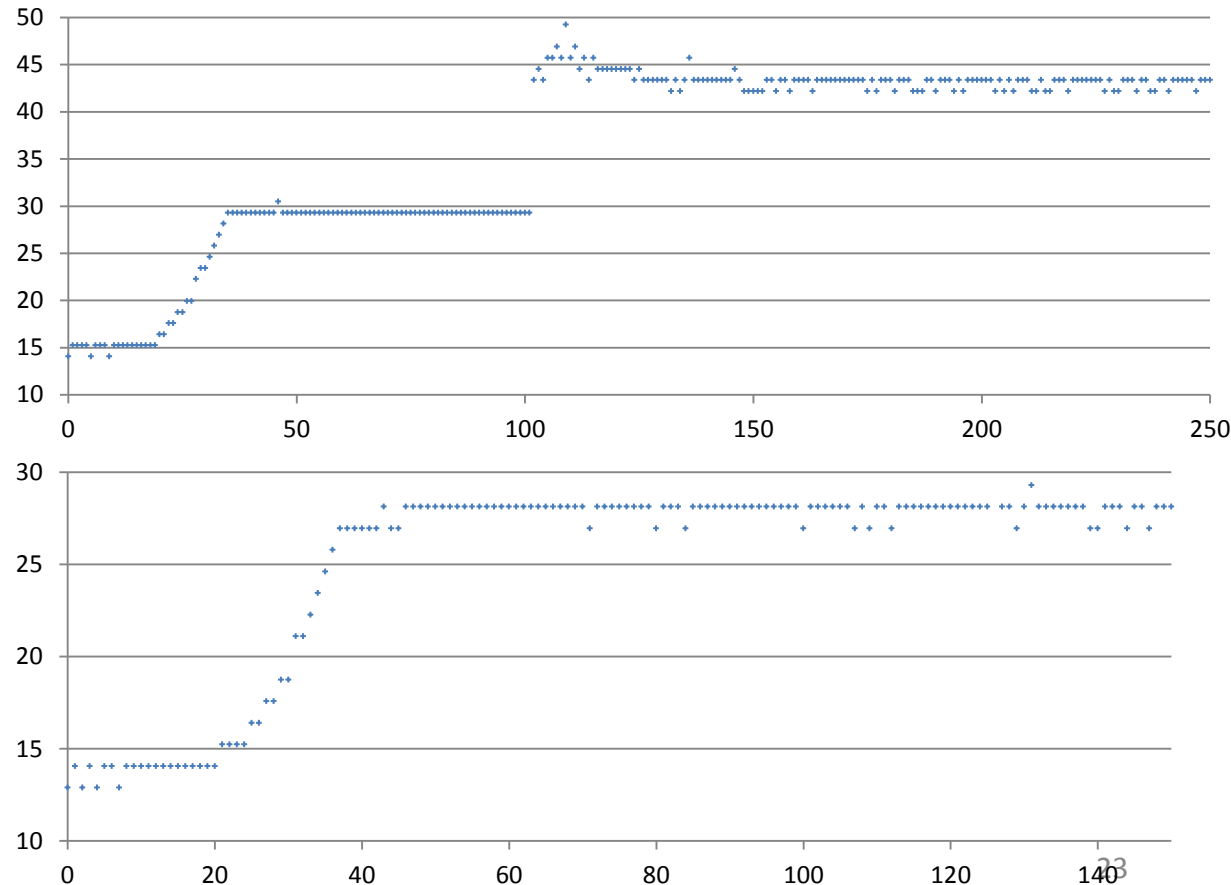
while (abs(angle-C) > 2)
{
    //Acceleration variable, a augmente
    a = 3*abs(Consigne-abs(angle-C))+5;
    //Serial.println("while");

    //Acceleration
    if (C>angle)
    {
        pwma += 5;
        analogWrite(Va,pwma);
        delay(a);
        angle = analogRead(pot);
        Serial.println(angle);
    }

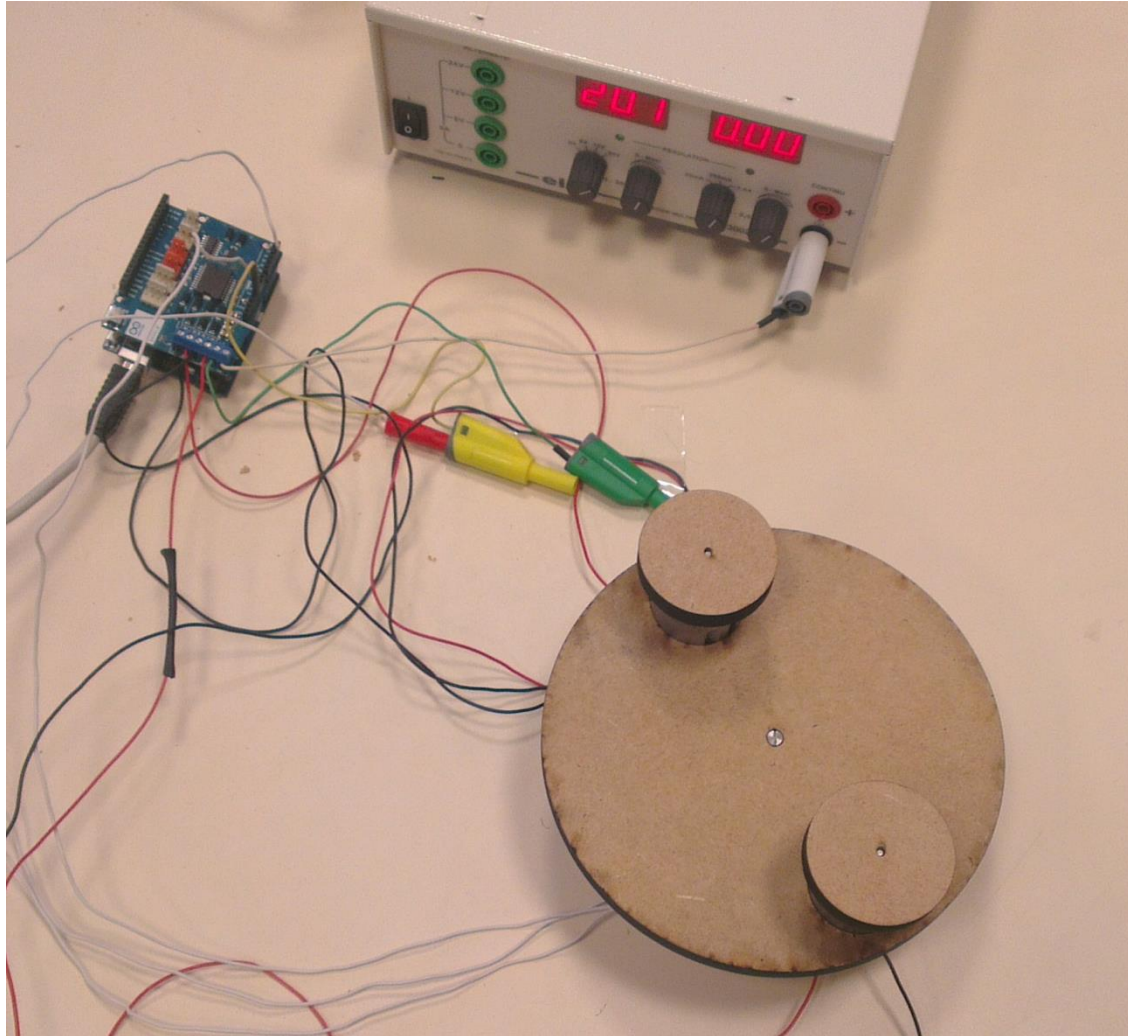
    //Arret
    if (pwma >= 250)
    {
        for (int i=0; i<=50; i++)
        {
            pwma -=5;
            analogWrite(Va,pwma);
            Serial.println(angle);
            delay(d); // on définit d p
        }
        pwma = 0;
        analogWrite(Va,pwma);
    }
}

```

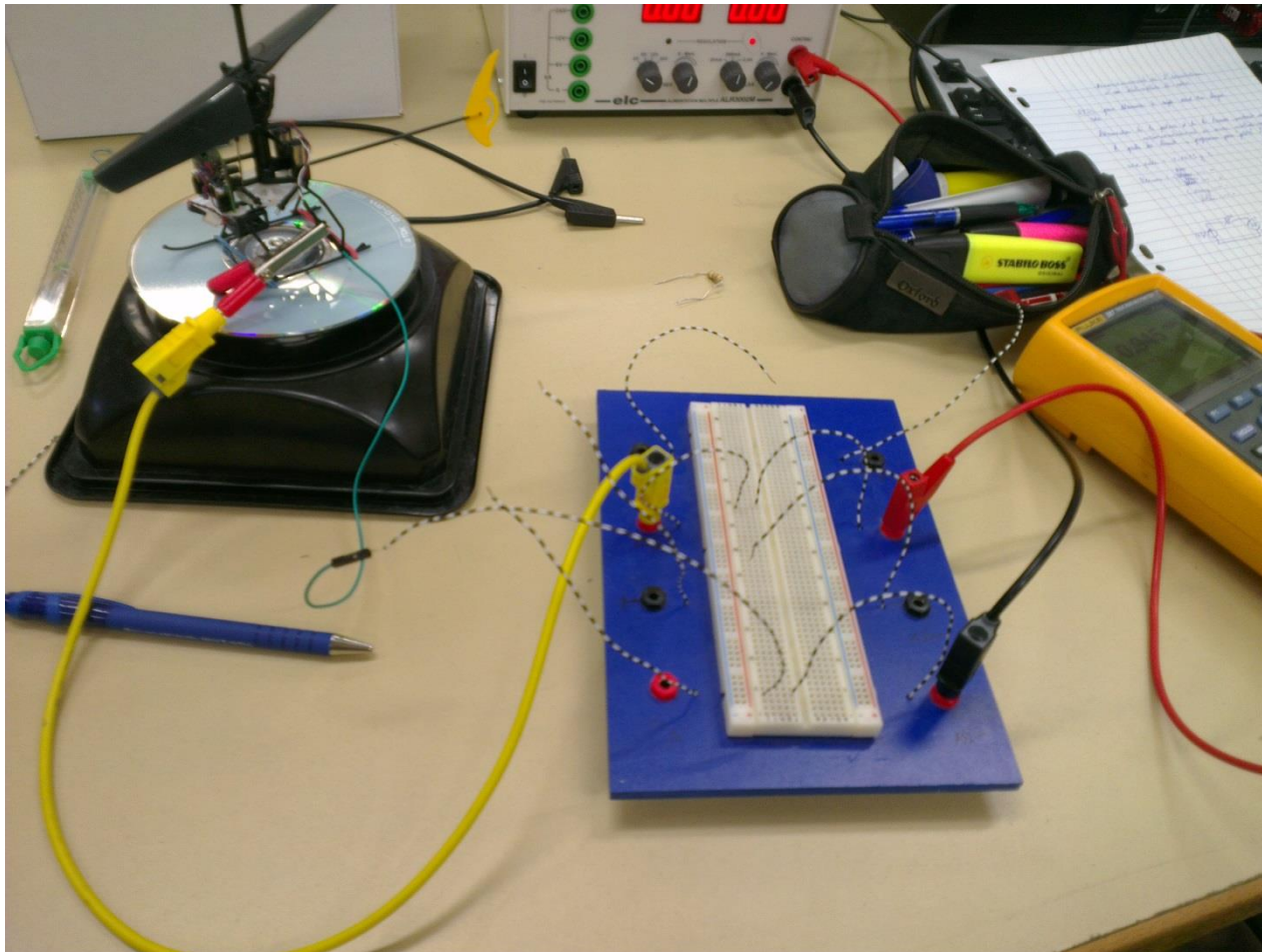
- Si l'angle est supérieur à la consigne, on accélère le moteur 1
- Quand le moteur tourne à la vitesse maximum, on l'arrête progressivement



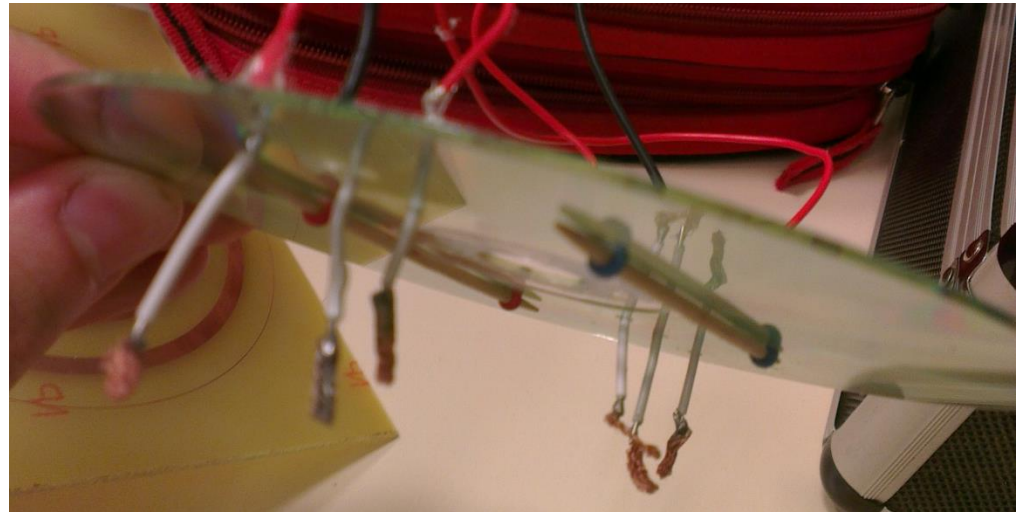
Conclusion



Annexe



Annexe



Annexe

